# Observation of Tungsten Line Emissions in Wavelength Range of 10 - 500 Å in Large Helical Device<sup>\*)</sup>

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Tungsten spectra have been observed in Large Helical Device (LHD) by injecting a coaxial tungsten pellet to identify the emission lines in extreme ultraviolet (EUV) range of 10 - 500 Å. The spectra of line emissions from tungsten ions have been measured in neutral-beam-heated discharges using two EUV spectrometers of EUV\_Short and EUV\_Long working in wavelength ranges of 10 - 130 Å and 50 - 500 Å, respectively. As a result, a lot of tungsten lines from low-ionized ions of  $W^{4+}$ ,  $W^{6+}$  and  $W^{7+}$  are observed for the first time in the toroidal device in addition to tungsten lines from highly ionized ions of  $W^{41+}$ - $W^{45+}$ . Measured line emissions are carefully identified based on the NIST database and the determined wavelengths show a good agreement with the NIST database. The result is summarized in table with information on blended lines obtained from the radial profile measurement.

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## 1. Introduction

In ITER (International Thermonuclear Experimental Reactor), which is a next-generation device for fusion research carrying out D-T burning plasma experiments, the tungsten material is used for plasma facing components (PFCs) in divertor region, since several positive characteristics are confirmed in the tungsten, i.e. high melting point, low sputtering yield and low tritium retention [1,2]. A spectroscopic study of tungsten becomes then important for understanding of the tungsten transport in core and edge plasmas and accurate determination of the radiative cooling rate.

A neutral tungsten emission, W<sub>I</sub>, observed in visible range at 4009 Å [3, 4] has been now widely used for the plasma wall interaction study [5,6]. Until now, any other lines from low ionized tungsten ions for the study of tungsten behavior in plasma edge have not been observed in the visible range above 4000 Å due to a lack of sufficient intensity. Line emissions from weakly ionized tungsten ions, W<sub>IV-VII</sub>, have been observed in vacuum ultraviolet (VUV) range of 500-1500 Å using a 3 m space-resolved VUV spectrometer with good spectral resolution [7]. The  $W_{XLV}$  $(W^{44+})$  and  $W_{XLVI}$   $(W^{45+})$  emissions have been already observed from many devices in extreme ultraviolet (EUV) range in the vicinity of 60 Å and 130 Å [8,9]. However, the spectral investigation of tungsten line emissions over the whole EUV wavelength range is still insufficient. In particular, tungsten spectral lines emitted in longer wavelength range, e.g. 200 - 500 Å, are not well examined because it is believed that tungsten lines probably do not exist in such a long wavelength range, while a soft x-ray spectrometer observing the wavelength range of 150-400 Å is planned to install on ITER for divertor diagnostics [10]. In order to accurately identify the tungsten spectral line over the entire EUV wavelength range, observations have been made not only for wavelength spectra but also for radial profiles in Large Helical Device (LHD) by injecting a coaxial graphite pellet with a small amount of tungsten [11]. Since LHD does not need any plasma current for plasma confinement, discharges are entirely tolerant for the impurity buildup. Therefore, the pellet injection with a variety of tungsten concentrations is possible in LHD. As a result, it is possible to generate a bright tungsten light source based on the LHD discharge with neutral beam injection (NBI). As the electron temperature of neutral-beam heated plasmas in LHD typically ranges in 1 keV  $\leq T_e \leq 4$  keV, most of line spectra from tungsten ions are emitted in the EUV range of 10 - 500 Å. The tungsten spectra in 10 - 500 Å are carefully identified and the result is summarized in a table. Several line emissions from low-ionized tungsten ions are newly found in longer wavelength range of 200 - 500 Å.

# 2. Experimental Setup

Two grazing-incidence EUV spectrometers called EUV\_Short [12] and EUV\_Long [13] are used for the present study to observe tungsten line emissions in the wavelength range of 10-130 Å and 50-500 Å, respectively. Both spectrometers have identical mechanical structures except for the grating and angle of incidence,

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i.e. a fixed entrance slit width of  $30 \,\mu\text{m}$ , a gold-coated concave varied-lines-spacing (VLS) laminar-type holographic grating and a back-illuminated charge-coupled device (CCD:  $1024 \times 255$  pixels,  $26 \times 26 \,\mu\text{m}^2$ /pixel). The VLS grating with 2400 grooves/mm (1200 grooves/mm) for EUV\_Short (EUV\_Long) requires the angle of incidence of 88.6° (87.0°). The wavelength spectrum is sequentially obtained at each 5 ms interval with full-binning mode in CCD. Both spectrometers are installed on #10-O port at a distance of ~10 m away from the plasma center and the tungsten pellet is also injected at the same port.

A space-resolved EUV spectrometer called EUV\_ Long2 [14] is installed for impurity profile measurement at wavelength range of 50 - 500 Å. The long axis of CCD is set perpendicular to the wavelength dispersion direction for the vertical profile measurement. The CCD is routinely operated in sub-image mode with five-pixel binning in the long axis and two-pixel binning in the short axis. The resultant CCD output signal shows an image of vertical profile versus wavelength with size of  $204 \times 127$  channels. The temporal resolution of EUV\_Long2 is generally 100 ms. The total vertical observation range in the profile measurement is nearly 0.5 m of which the range corresponds to half the vertical plasma diameter at the horizontally elongated plasma cross section.

#### **3. Experimental Results**

A series of experiments on the tungsten spectroscopic study have been done in LHD with tungsten pellet injection. A coaxial-structured tungsten pellet with a thin tungsten wire inserted into a polyethylene or graphite cylindrical tube is injected to NBI hydrogen discharges with speed of ~200 m/s. The tungsten spectra in EUV range are measured in hydrogen discharges at magnetic axis position of  $R_{ax} = 3.6$  m and toroidal magnetic field of  $B_T = -2.75$  T. The minus sign of  $B_T$  means magnetic field in counterclockwise direction.

A typical discharge with tungsten pellet injection is shown in Fig. 1. The pellet is injected at t = 4.33 s. As the tungsten wire with 0.05 mm diameter and 0.7 mm length is used in the discharge, the number of injected tungsten atoms is approximately  $8.6 \times 10^{16}$ . The discharge is maintained by three negative-ion-source-based NBIs (n-NBI#1-#3) with energy of 180 keV during 3.6-6.2 s and two positive-ion-source-based NBIs (p-NBI#4-#5) with energy of 40 keV during 6.2 - 8.2 s, as shown in Fig. 1 (a). Lineaveraged electron density,  $n_{\rm e}$ , central electron temperature,  $T_{e0}$ , total radiation power,  $P_{rad}$ , and plasma stored energy,  $W_p$ , are shown in Figs. 1 (b) - 1 (e), respectively. After tungsten pellet injection,  $n_e$  and  $P_{rad}$  quickly increase, while  $T_{e0}$  slowly decreases and  $W_p$  stays almost constant. The  $T_e$  and  $n_e$  profiles at different discharge timings during t = 4.3 - 5.2 s are shown in Figs. 2 (a) and 2 (b), respectively. Data at t = 4.3 s indicates  $T_e$  and  $n_e$  profiles just before the tungsten pellet injection. Although the  $T_{\rm e}$  de-



Fig. 1 Time behaviors of (a) port-through NBI power, (b) lineaveraged electron density, (c) central electron temperature, (d) total radiation power and (e) plasma stored energy. A coaxial pellet with tungsten wire size of  $0.05 \text{ mm}^{\phi} \times 0.7 \text{ mm}^{L}$  is injected at t = 4.33 s.



Fig. 2 Temporal evolutions of radial profiles of (a) electron temperature and (b) electron density just before (t = 4.3 s) and after (4.4 - 5.2 s) the pellet injection.

creases and the  $n_e$  increases after the tungsten pellet injection, both radial profiles are almost unchanged. It indicates that the tungsten injection does not disturb so much the discharge condition.

The tungsten spectra at wavelength range of 10-



Fig. 3 EUV spectra of tungsten emission lines observed in LHD at (a) 10 - 35 Å, (b) 35 - 55 Å, (c) 55 - 90 Å, (d) 90 - 120 Å, (e) 120 - 155 Å, (f) 155 - 190 Å, (g) 190 - 225 Å, (h) 225 - 260 Å, (i) 260 - 295 Å, (j) 295 - 330 Å, (k) 330 - 365 Å, (l) 365 - 400 Å, (m) 400 - 435 Å, (n) 435 - 470 Å and (o) 470 - 500 Å.

500 Å observed with EUV\_Short and EUV\_Long spectrometers are carefully identified based on NIST atomic spectra database and previous studies [8, 15, 16], as shown in Figs. 3(a) - 3(o). The shot number, central electron temperature and data acquisition timing after pellet injection are indicated for each spectrum. The spectra in Figs. 3 (a) and 3 (b) are measured by EUV\_Short with spectral resolution of 0.051 Å at  $\lambda = 25$  Å and 0.067 Å at  $\lambda = 45$  Å. The spectra in Figs. 3 (c) - 3 (o) are measured by EUV\_Long with spectral resolution of 0.149 Å at  $\lambda =$ 105 Å and 0.270 Å at  $\lambda = 450$  Å. Therefore, the uncertainty in the spectral wavelength determination is estimated to be 0.005 Å for short wavelength range and 0.015 - 0.03 Å for long wavelength range of which the values are calculated as one tenth of the spectral resolution. In Fig. 3, the tungsten line emissions are denoted with dotted arrows and line emissions from other impurity ions are denoted with solid arrows. The wavelength scale in abscissa of Fig. 3 is determined by linear interpolation and extrapolation based on the accurate wavelengths of well-known transitions in C, O, N and Fe impurity ions.

Two tungsten unresolved transition arrays (UTAs) appear at wavelength ranges of 19-35 Å and 48-53 Å as shown in Figs. 3 (a) and 3 (b), respectively. The UTA spectra are replotted in detail against different temperatures of  $T_{e0} = 0.42, 0.87, 1.63, 1.94$  and 2.45 keV as shown in Figs. 4 (a) - 4 (e), respectively. The UTA spectra composing of many tungsten ions largely move to shorter wavelength range with increase in  $T_e$  showing an increase in the ionization stage of tungsten ions and finally almost disappear when the  $T_e$  is sufficiently high (see Fig. 4(e)). As one can see from the figures, a simple spectral identification of the UTA is quite difficult. In the present study, therefore, the UTA spectra are excluded from a summary table described later. Recently, on the other hand, the UTA spectrum at 19-35 Å is attempted to understand by superposing two UTA CoBIT spectra [8]. A model calculation is also carried out to explain the LHD UTA spectrum [17]. In addition, the ionization stage of tungsten ions is determined at each wavelength interval of the UTA based on the



Fig. 4 Tungsten UTA spectra at central electron temperatures of (a) 0.42, (b) 0.87, (c) 1.63, (d) 1.94 and (e) 2.45 keV.

profile measurement [16].

Tungsten line emissions from highly ionized ions are observed at  $T_{e0} = 2.66 \text{ keV}$ , as shown in Figs. 3 (c) and 3 (e). These spectra are taken at 0.42 s after the pellet injection. The wavelength of a line emission identified as W<sup>44+</sup> located at 60.93 Å [18] is re-examined and determined to be 60.87 Å in this study as shown in Fig. 3 (c), while the line emission is clearly broadened. It is investigated in a previous experimental work [19] that the W<sup>44+</sup> line is blended with W<sup>42+</sup> and W<sup>43+</sup> line emissions. A line emission theoretically predicted as W<sup>45+</sup> at 62.187 Å [18] is identified at a wavelength of 62.188 Å in this study, where the uncertainty in wavelength determination is  $\sim 0.007$  Å, while it is observed at 62.336 Å in a previous experimental work [18]. This emission line is also blended with tungsten emissions in lower ionization stages [19]. The blended line is estimated to be W39+ at 62.366 Å in EBIT result [18] and to be W<sup>44+</sup> in HULLAC code [8]. Three line emissions measured at 126.29 Å, 126.998 Å, and 131.21 Å are identified as a single ionization of W43+, W45+, and W41+, respectively [19, 20]. A line emission measured at 129.45 Å in Fig. 3 (e) is identified as W<sup>42+</sup> [20, 21]. A line emission measured at 132.88 Å is identified as W<sup>44+</sup> [20, 21]. It can be easily found because the intensity is very strong.

In the present identification mentioned above the reliability is also checked with the radial profile measured along the vertical direction. As an example of the profile measurement, vertical profiles of W<sup>43+</sup> (126.05 Å  $\leq \lambda \leq 126.37$  Å), W<sup>41+</sup> (130.93 Å  $\leq \lambda \leq 131.25$  Å) and W<sup>44+</sup> (132.72 Å  $\leq \lambda \leq 133.06$  Å) obtained with EUV\_Long2 are plotted in Fig. 5. The emission lines at 126.05 - 126.37 Å and 130.93 - 131.25 Å are found not to





Fig. 5 Vertical profiles of  $W_{XLII}$  ( $W^{41+}$ ) (dotted line: 130.93 Å  $\leq \lambda \leq 131.25$  Å),  $W_{XLIV}$  ( $W^{43+}$ ) (solid line: 126.05 Å  $\leq \lambda \leq 126.37$  Å) and  $W_{XLV}$  ( $W^{44+}$ ) (dashed line: 132.72 Å  $\leq \lambda \leq 133.06$  Å). The  $W_{XLV}$  is blended with Fe<sub>XX</sub> at 132.850 Å.

be blended with emission lines from intrinsic impurities in the LHD plasma, due to the centrally peaked profile. However, the vertical profile extracted at 132.72 - 133.06 Å is clearly different having a shoulder at Z = 0.3 m. The blended line is estimated to be Fe<sup>19+</sup> at 132.850 Å because the  $T_e$  at the shoulder position is close to the ionization energy of Fe<sup>19+</sup> ions.

A lot of EUV line emissions from low-ionized tungsten ions of W<sup>4+</sup>, W<sup>6+</sup> and W<sup>7+</sup>, are clearly observed at long wavelength range of 155 - 500 Å just after the tungsten pellet injection. A time duration at which such line emissions can be observed with relatively strong intensities is very short, e.g. 15 ms corresponding to 3 CCD frames. Until now W<sub>VIII</sub> spectra are observed at 175 - 275 Å in MT-IM tokamak without identification due to a poor spectral resolution of 5 Å at [22]. The W<sub>VIII</sub> spectra are also studied in EBIT device and calculation [23-25]. In LHD, W<sub>VIII</sub> lines are clearly found at 155 - 295 Å in Figs. 3 (f) - 3 (i). However, those spectra are entirely different from EBIT spectra. The reason seems to originate in a different density between two devices. There are many data on lowionized tungsten in the NIST atomic spectra database [15]. In practice, most of these data originate in the spark experiment [26–29] and the tungsten spectra observed from the spark plasma with spectral resolution of 0.01 Å are similar to the LHD spectra.

The W<sub>V</sub> and W<sub>VII</sub> lines can be identified at 295 - 500 Å in Figs. 3 (j) - 3 (o). The W<sub>VII</sub> spectra are mainly studied at 180 - 450 Å in the SSPX spheromak and calculation due to less data from EBIT [25–27]. However, the spectra are also quite different from LHD spectra due to the same reason as EBIT. A study is also done at 180 - 450 Å in spark device on W<sub>VII</sub> [26, 27] and W<sub>V</sub> [28, 29]. The W<sub>V</sub> and W<sub>VII</sub> spectra from the spark are also identical to the LHD spectra.

The tungsten emission lines observed at 10-500 Å in the present study are summarized in Table 1 except for the

Table 1 Summary of spectral identification of tungsten line emissions. The first column shows tungsten ionization stage and the second and third columns give the wavelengths of line emissions from NIST database and the present observation, respectively. Discrepancy between  $\lambda_{\text{NIST}}$  and  $\lambda_{\text{obs}}$  and relative spectral intensity are shown in the fourth and fifth columns, respectively. The status in the sixth column of 'Single' or 'Blended' means the emission line consists of a single ionization stage or is blended with other emission lines.

$W^{q^+}$	$\lambda_{\rm NIST}$ (Å)	$\lambda_{\rm obs}$ (Å)	$\lambda_{ m NIST}$ - $\lambda_{ m obs}$	Intensity	Status
			(Å)	(counts/5ms)	
WV (W <sup>4+</sup> )	395.575	395.571	0.004	1077	Single
	422.458	422.421	0.037	3523	Single
	430.643	430.629	0.014	1355	Blended
					(Fe <sup>4+</sup> )
	476.906	476.919	-0.013	553	Single
WVII (W <sup>6+</sup> )	324.054	324.098	-0.044	866	Single
	339.827	339.749	0.078	1407	Blended
	339.841	339.992	-0.151	1233	Blended
	340.183	340.235	-0.052	1243	Blended
	489.064	489.099	-0.035	445	Single
	495.503	495.509	-0.006	889	Single
	496.897	496.906	-0.009	564	Single
WVIII (W <sup>7+</sup> )	160.940	160.998	-0.058	26330	Single
	168.381	168.405	-0.024	10560	Single
	201.288	201.266	0.022	9240	Single
	202.250	202.249	0.001	4341	Single
	203.623	203.630	-0.007	3864	Single
	240.634	240.667	-0.033	2180	Single
	248.765	248.765	0	7307	Single
	260.146	260.241	-0.095	3148	Single
WXLII (W <sup>41+</sup> )	131.21	131.25	-0.04	1522	Single
WXLIII (W42+)	129.41	129.45	-0.04	2084	Blended
WXLIV (W43+)	126.29	126.21	0.08	1651	Single
WXLV (W <sup>44+</sup> )	60.93	60.87	0.06	7387	Blended
					$(W^{42^+}, W^{43^+})$
	132.88	132.90	-0.02	16051	Blended
					(Fe <sup>19+</sup> )
WXLVI (W <sup>45+</sup> )	126.998	127.017	-0.019	1752	Single
	62.336	62.188	0.148	4707	Blended

UTA lines. In Table 1, the first column shows the tungsten ionization stage, and the second and third columns give the wavelengths from NIST database and the present observation, respectively. As described above the NIST data are based on identification results from the spark experiment. Discrepancies between  $\lambda_{\text{NIST}}$  and  $\lambda_{\text{obs}}$  indicated in the fourth column are obviously smaller than 0.1 Å for all observed emission lines except for two lines at  $\lambda_{obs}$  = 62.188 Å and  $\lambda_{obs} = 339.992$  Å. The reason is due to a large influence from blended lines. The intensity at the spectral peak is shown in the fifth column. The  $W_{VIII}$  line at  $\lambda_{obs}$ = 160.998 Å is found to be the strongest in the wavelength range of 155 - 500 Å. The  $W_V$  and  $W_{VII}$  intensities are relatively weak and many lines are blended with other lines. The status of observed tungsten lines is denoted in the sixth column. In the case of 'Blended' ionization stages of the blended lines are also indicated.

### 4. Summary

Tungsten spectra are observed at wavelength range of 10 - 500 Å by injecting a coaxial tungsten impurity pellet

in LHD. Two tungsten UTAs are observed at wavelength range of 10-55 Å. The UTA at 19-35 Å moves toward shorter wavelength side with electron temperature and the UTA at 48 - 53 Å consisting of W<sup>24+</sup>-W<sup>33+</sup> ions gradually disappear with electron temperature. The UTA almost disappear at sufficiently high-temperature phase, e.g.  $T_{e0} =$ 2.66 keV and line emissions from highly ionized tungsten ions begin to be observed at 55 - 155 Å. Blended line emissions are examined by measuring the radial profile. A lot of line emissions from low-ionized tungsten ions of W<sup>4+</sup>, W<sup>6+</sup> and W<sup>7+</sup> are clearly observed at 155 - 500 Å just after the tungsten pellet injection and identified based on the NIST database. All these line emissions are observed for the first time in the toroidal device, while the NIST data are based on the result from spark plasmas. The tungsten emission lines observed at 10-500 Å are summarized in the table except for the UTA lines. The present identification shows a good agreement with the NIST data base. In particular, tungsten spectra from low-ionized ions observed for the first time in the toroidal device will contribute to the tungsten impurity diagnostics in fusion research in addition to the accuracy improvement of atomic structure modeling.

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