## §16. High Energy Ion Component Measurement by ICRF Power Modulation Method

Torii, Y. (Nagoya Univ.), Kumazawa, R.

As the confinement time of high energy ions is much different between in  $R_{ax}$ =3.6m and in  $R_{ax}$ =3.75m, a different ratio of the stored energy of the high energy ions to that of the bulk plasma can be experimentally observed. An analysis in the plasma discharge with the RF power modulation gives the tail fraction of high energy ions by measuring phase difference among the total stored energy  $\delta W_p$ , the bulk plasma stored energy  $\delta W_b$  and the ICRF heating power  $\delta P_A$ . The relations between  $\delta W_p$  and  $\delta W_b$  and between  $\delta P_A$  and  $\delta W_p$  are derived from the power balance equation and expressed in the following complex equations,  $\delta W_p = 3$ 

$$\frac{\delta w_{p}}{\delta W_{b}} = 1 + \frac{3}{2} \frac{A R_{tb}}{\eta_{trns}} + i \frac{3}{2} \omega \tau_{se0} / 2,$$

$$\frac{\delta W_{p}}{\delta P_{A}} = \eta_{trns} \tau_{se0} / 2 \eta_{0} \frac{1 + \frac{3}{2} (i \omega \tau_{se0} / 2 + \frac{A R_{tb}}{\eta_{trns}})}{-B R_{tb} + (i \omega \eta_{trns} \tau_{se0} / 2 + 1) (i \omega \tau_{se0} / 2 + \frac{A R_{tb}}{\eta_{trns}})},$$

$$R_{tb} = \frac{\tau_{\epsilon}^{tail}}{\tau_{E}}, \quad A = \frac{3}{2} + (1 - \beta), \quad B = \frac{\eta' T_{0}}{\eta_{0}} + \frac{3}{2}.$$

Here the energy transfer from the high energy ions to helium ions is neglected.  $R_{tb}$  is a ratio of the stored energy of the high energy ions to that of the bulk plasma.  $\omega$  and  $\beta$  are an applied modulation frequency and a numerical factor derived from the dependence of the energy confinement time on the temperature, *i.e.*,  $\tau_E \propto \tau_{E0} T^{\beta}$ ;  $\beta$ =-1.44 derived from ISS95.  $\eta_0$  is a heating efficiency and  $\eta$ ' is its derivative of temperature<sup>1</sup>. The phase difference  $\theta_{pb}$  between  $\delta W_p$  and  $\delta W_b$ , and the phase difference  $\theta_{pA}$  between  $\delta W_p$  and  $\delta P_A$  are given in the following equations;

$$\tan \theta_{pb} = \frac{\frac{3}{2}W}{1 + \frac{AR_{tb}}{\eta_{trns}}},$$
  
$$\tan \theta_{pA} = -W \frac{(A + \frac{3}{2}B)R_{tb} + 1 + \frac{3}{2}(AR_{tb})^2 + \frac{3}{2}W^2}{(\frac{A}{\eta_{trns}} - B)(1 + \frac{3}{2}\frac{AR_{tb}}{\eta_{trns}})R_{tb} + (\frac{3}{2} - \eta_{trns})W^2}, \quad W = \omega\tau_s/2.$$

A relation between  $\theta_{pA}$  and  $\theta_{pb}$  is obtained in the following equation by substituting  $\tan \theta_{pb}$  instead of  $\omega \tau_s/2$ ;

$$\tan \theta_{pA} = -\frac{2}{3} \tan \theta_{pb} (1 + \frac{AR_{tb}}{\eta_{trns}})$$

$$\times \frac{(A + \frac{3}{2}B)R_{tb} + 1 + \frac{3}{2}(AR_{tb})^2 + \frac{2}{3}(\tan \theta_{pb}(1 + \frac{AR_{tb}}{\eta_{trns}}))^2}{(\frac{A}{\eta_{trns}} - B)(1 + \frac{3}{2}\frac{AR_{tb}}{\eta_{trns}})R_{tb} + (\frac{3}{2} - \eta_{trns})(\frac{2}{3}\tan \theta_{pb}(1 + \frac{AR_{tb}}{\eta_{trns}}))^2}.$$

 $\theta_{pA}$  was calculated as a function of  $R_{tb}$  at five different  $\theta_{pb}$ ,  $\theta_{pb}$ =10°, 15°, 20°, 25°, and 30° and plotted in Fig.1.  $\theta_{pA}$  increases with  $R_{tb}$  when  $R_{tb} < 0.2$ , reaches its maximum at

 $R_{tb} = 0.2$  and decreases with  $R_{tb}$  at  $\theta_{pb}=10^{\circ}$ .  $\theta_{pb}$  depends on  $\omega \tau_s/2$ ; it increases with  $T_e$  and with decrease in  $n_e$ . The relation between  $\theta_{pA}$  and  $\theta_{pb}$  is calculated as a parameter of  $R_{tb}$ . Loci of  $R_{tb}$  of 0.01, 0.1, 1.0 and 10.0 are plotted in the plane of  $\theta_{pb}$  and  $\theta_{pA}$  as shown in Fig.2. It should be noted that the pressure ratio of  $R_{tb}$  can be deduced from the measurement of  $\theta_{pA}$  and  $\theta_{pb}$ .



Fig.1 Dependence of a phase difference between  $W_p$  and  $P_A$  on the pressure ratio of  $R_{tb}$  as the parameter of  $\theta_{pb}$ .



Fig.2 Dependence of a phase difference between  $W_p$  and  $P_A$  on a phase difference between  $W_p$  and  $W_b$  as the parameter of the pressure ratio of  $R_{tb}$ .

Reference

1) Y. Torii, et. al., Plasma Physics and controlled Fusion, 43 (2001) 1191.